

MIE-MPI, Mathematics for Informatics - Homework no. 3

Instructions:

- You should try to solve all the exercises. Even if you do not do all the exercises, you can get all the points.
 - Sign every paper of your solution on the top of the page along with the number of the homework.
 - Presentation is taken into account; correct results themselves are not enough. The reasoning on how the result was found should be clearly visible.
 - Comment your calculations in a reasonable way: the reader should understand what you do and *why*. The solution should be “possible to read”, not “needed to decrypt”.
 - Do not answer unasked questions. It is important to know what is needed to solve the problem and what is not needed.
 - If you use a result from another source than the lectures and tutorials, cite your source properly (do not forget to cite used software if applicable).
 - The homework is a preparation for the next written test.
 - The homework is collected at the lecture (Tuesday 17/12/2019). If you cannot come, you can use the mailbox at the Department of Applied Mathematics, 14th floor of building A. In the latter case, send me an email at francesco.dolce@fjfi.cvut.cz before the deadline.
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Exercise 1. Say which of the following numbers are normalized machine numbers in single precision (`binary32`) or in double precision `binary64`. When is the case, represent them (using the standard `IEEE-754`).

- 10^{1234} ;
- 10^{-2000} ;
- $10 + \frac{5}{8}$;
- 4^{10} ;
- 4^{-10} ;
- $\frac{3}{5}$;
- $7 + \frac{1}{7}$;
- $7 + \frac{1}{8}$;
- 2^{-1280} ;

- 2^{-128} .

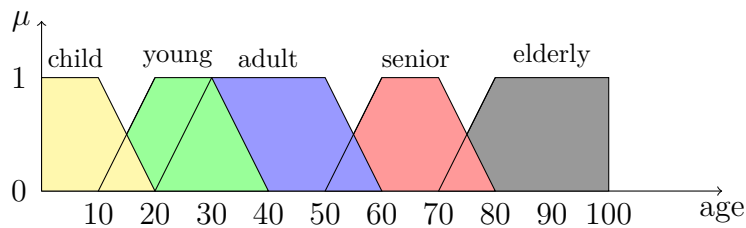
Exercise 2. What are the normalized machine numbers which are the closed neighbours of 0?

Exercise 3. Is it true that $\text{fl}(x + y) = \text{fl}(x) + \text{fl}(y)$? Justify your answer (i.e., give an argument or find a counterexample).

Exercise 4. Prove that the following binary operation is a t-norm:

$$x \star y = \begin{cases} y & \text{if } x = 1, \\ x & \text{if } y = 1, \\ 0 & \text{otherwise.} \end{cases}$$

Exercise 5. Let us consider the 5 fuzzy sets in the following picture: *child*, *young*, *adult*, *senior*, *elderly*.



Write the definition and draw the graph of the membership function of the fuzzy sets “**young-adult**” defined as “*young*” \cap “*adult*” using the following t-norms:

- product,
- Gödel,
- Łukasiewicz.

Exercise 6. Using the picture and the fuzzy sets of the previous exercise (and De Morgan’s law) write the definition and draw the graph of the membership function of the fuzzy set “**wise**” defined as “*senior*” \cup “*elderly*” using the following t-norms:

- product,
- Gödel,
- Łukasiewicz.