Contribution Title: Authors: Presenting author: Affilation: E-mail: Invited speaker: YRS seminar: RECENT PROGRESS ON WAVE-MAPS P. Raphael, I. Rodnianski, J. Sterbenz, D. Tataru Sterbenz J. UCSD jsterben@math.ucsd.edu Topical session NO

In this talk I will discuss recent progress on the so called Wave-Maps which are perhaps the simplest non-linear hyperbolic gauge field equations. These include maps into the sphere  $\mathbb{S}^2$ , also sometimes called "sigma-models" which arise in quantum-field theory and ferromagnetism, as well as maps into the hyperbolic plane  $\mathbb{H}^2$ , which can be thought of as models for certain gravitational fields with U(1) symmetry. Based on numerical experiments and analogies with the harmonic-map heat-flow, it has long been conjectured that such fields could become singular for positively curved targets, while for negative target curvature the Cauchy-problem should always be globally well posed. There has been striking progress recently on this set of conjectures, and I will try give some idea about the current state of affairs in my talk.

This is joint work with Pierre Raphael, Igor Rodnianski, and Daniel Tataru, and I will also discuss recent work of Joachim Krieger, Wilhelm Schlag, and Terry Tao, as well as earlier seminal contributions by Sergiu Klainerman, Matei Machedon, and others.